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SEMI MICROSCOPIC DESCRIPTION OF 84Kr

H. Dias

Instituto de Física, Universidade de São Paulo

F. Krmpotić

Departamento de Física, Facultad de Ciências Exactas, Universidad Nacional de La Plata, c.c. 67, Argentina and Instituto de Física, Universidade de São Paulo, São Paulo, Brasil

L. Losano

Instituto de Física, Universidade de São Paulo

R.C. Mastroleo

Divisão de Física Teórica, Instituto de Estudos Avançados, Centro Técnico Aeroespacial, 12200 São José dos Campos, SP, Brasil

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### H. DIAS

INSTITUTO DE FÍSICA DA UNIVERSIDADE DE SÃO PAULO

# F. KRMPOTIC+

DEPARTAMENTO DE FÍSICA, FACULTAD DE CIÊNCIAS EXACTAS, UNIVERSIDAD NACIONAL DE LA PLATA, C.C. 67, ARGENTINA AND INSTITUTO DE FÍSICA DA UNIVERSIDADE DE SÃO PAULO, SÃO PAULO, BRASIL

### L. LOSANO++

INSTITUTO DE FÍSICA DA UNIVERSIDADE DE SAO PAULO, SP, BRASIL

## R.C. MASTROLEO+++

DIVISÃO DE FÍSICA TEÓRICA, INSTITUTO DE ESTUDOS AVANÇADOS, CENTRO TECNICO AEROESPACIAL, 12200, SÃO JOSÉ DOS CAMPOS, SP, BRASIL

- +++Present Address: Department of Physics, University of Texas,
  Austin, Texas, 78712, U.S.A.
- ++Permanent Address. Departamento de Fisica da Universidade Fe deral da Paraiba, João Pessoa, Paraiba
- \*Member of the Carrera del Investigador Cientifico, Consejo Nacional de Investigaciones Cientificas y Tecnicas, Argentina

#### ABSTRACT

The experimental information on the  $^{84}$ Kr nuclei is compared with the model calculation in which two neutron holes are coupled to the vibrational field. Based on the lower-order terms of a perturbative expansion of the E2 and M1 transition matrix elements, a simple rule is obtained for the sign and the magnitude of the  $\delta$  (E2/M1) ratios for the transitions between the second and first  $2^+$  states in some vibrational nuclei.

[Nuclear structure  $^{84}$ Kr, calculated levels J,  $\pi$  and  $\delta$  (E2/M1). Cluster-phonon model. Pairing interaction].

#### I. INTRODUCTION

The directional correlations of coincident  $\gamma$  transitions have recently been measured for several cascades in the  $^{84}$ Kr nucleus  $^{1)}$ . Besides establishing spins of a number of levels, this measurement also gives information on the multipole mixing ratios  $\delta$  (E2/M1), which is of considerable importance in providing a better understanding of the structure of this nucleus.

More specifically, while the spins and parities of the low-lying states of <sup>84</sup>Kr indicate a collective quadrupole vibrational structure, the predominance of Ml in the multipolarity of several gamma transitions strongly suggests that also the single-particle degrees of freedom play an inportant role.

In view of the above-mentioned properties we propose in the present work a theoretical interpretation of the structure of  $^{84}$ Kr nucleus, and in particular of the ratios  $_{6}$  (E2/M1) measured in Ref. 1, within the two-hole cluster-quadrupole vibration coupling model.

#### II. THE NUCLEAR MODEL AND PARAMETERS

A detailed description of the model is given in Refs. 2 and 3. Here we only sketch the main formulas in order to establish the notation. The system is described by the Hamiltonian

$$H = H_0 + H_{res} + H_{int}$$
 (1)

where  ${\rm H_O}$  is the energy of the unperturbed system represented by a quadrupole vibrational field and by two valence neutrons in a central field. The residual interaction energy among the neutrons in the shell-model cluster,  ${\rm H_{res}}$ , only includes explicitly the pairing force. The particle-vibration interaction is given by the expression

$$H_{int} = -\frac{\beta_2}{\sqrt{5}} \sum_{\mu} \left[ b_2^{\mu +} + (-)^{\mu} b_2^{-\mu} \right] \sum_{i=1}^{2} k(r_i) y_{2\mu}^{*}(\theta_i, \phi_i)$$
 (2)

where  $k\left(r\right)$  is the interaction intensity and  $\beta_{2}$  is the quadrupole deformation parameter.

The eigenvalue problem is solved in the basis  $| \int (j_1 j_2) J, NR | I> , \text{ where } j = (n \ell j) \text{ stands for the quantum numbers of the hole states, } J \text{ is the total angular momentum of the two holes, } N \text{ and } R \text{ represent the phonon number and the angular momentum, } respectively, and I is the total angular momentum.}$ 

 $\hbox{ The matrix elements of $H_{\hbox{\scriptsize int}}$ are parametrized by }$  the coupling constant a defined as

$$a = \frac{\langle k \rangle \beta_2}{\sqrt{20\pi}} \tag{3}$$

where <k> is the mean value of the radial matrix element of the interaction.

The electric quadrupole and magnetic-dipole

operators consist of a particle and a collective part

$$M(E2,\mu) = e_{p}^{eff} \sum_{i=1}^{2} r_{i}^{2} Y_{2\mu}(\theta_{i},\phi_{i}) + \frac{3R_{o}^{2}}{4\pi} e_{v}^{eff} \left[ b_{2}^{\mu+} + (-)^{\mu} b_{2}^{-\mu} \right], \quad (4)$$

$$M(ML, \mu) = (\frac{3}{4\pi})^{1/2} \left[ g_R^R R_{\mu} + g_{\ell}^L L_{\mu} + g_{g}^S L_{\mu} \right] \mu_N , \qquad (5)$$

where e<sup>eff</sup><sub>p</sub> is the effective particle charge,  $e_V^{eff} = Ze\beta_2/\sqrt{5}$  is the effective vibrator charge, and  $g_R$ ,  $g_Q$  and  $g_S$  are, respectively, the collective, orbital and spin gyromagnetic ratios.

The mixing ratio  $\delta \, (\text{E2/M1})$  for the E2 and M1 transitions reads  $^{4)}$ 

$$\delta (E2/M1) = 0.835 (E_{\gamma}/MeV) (D/eb\mu_N^{-1})$$
 (6)

with

$$D = \frac{\langle I_{i} | | M(E2) | I_{f} \rangle}{\langle I_{i} | | M(M1) | I_{f} \rangle}$$
(7)

The matrix elements of the E2 and Ml operators are expressed in the forms

$$\langle I_{\underline{i}} | M(E2) | | I_{\underline{f}} \rangle = (e_{\underline{p}}^{eff} A + e_{\underline{v}}^{eff} B) eb,$$
 (8a)

$$= (g_{S}C + g_{\ell}D + g_{R}E)\mu_{N}$$
 (8b)

and the quantities A, B, C, D and E are calculated from the model wave functions.

The Hamiltonian was diagonalized with the following set of parameters:

- (a) pairing strength G = 0.29 MeV, which follows from the estimate of Kisslinger and Sorensen<sup>5)</sup> (G = 25/A MeV);
- (b) phonon energy  $\hbar\omega_2$  = 1.56 MeV, is the experimental energy of  $2^+_1$  state in the single-closed-shell  $^{86}Kr$  nucleus  $^6)$  ;
- (c) particle-vibration coupling constant a = 0.74 MeV, which results from  $\beta_2$  = 0.13 (as measured in the Coulomb excitation process on  $^{86}$ Kr (ref. 6)) and  $^{4}$ Kr (as estimated numerically using wave functions obtained from the Woods-Saxon potential  $^{7}$ );
- (d) single particle energies  $\epsilon_{g_{9/2}} = 0$ ,  $\epsilon_{p_{1/2}} = 0.80$  MeV,  $\epsilon_{p_{3/2}} = 1.35$  MeV and  $\epsilon_{f_{5/2}} = 1.8$  MeV, were taken from the work of Boer et al<sup>8</sup>.

In this parametrization, without an adjustable parameter, we diagonalize the Hamiltonian by including all the vibrational states up to three phonons.

The eletromagnetic properties were evaluated with the usual values of the effective eletric charge and effective gyromagnetic ratios.

$$e_p^{eff} = 0.5e$$
,  $e_v^{eff} = \frac{\beta_2 Ze}{\sqrt{5}} = 2.09$ ,  $g_R = Z/A = 0.43$ ,  $g_\ell = 0$ ,  $g_s^{eff} = 0.6g_s^{free} = -2.30$ 

#### III - RESULTS AND DISCUSSION

In order to test the parametrization quoted in the previous section we first breafly discuss the available experimental data for the N = 49 nuclei $^{9-12}$ ). The energy spectra are compared in Fig. 1 and the results for the electric quadrupole and magnetic dipole moments of the ground state are shown in Table I. It showld be noted that the agreement between the calculated and the measured energy spectra for  $^{85}$ Kr,  $^{87}$ Sr,  $^{89}$ Zr and  $^{91}$ Mo nuclei can be improved by lowering the particle-phonon coupling constant. As an example, in Fig. 1 is also exhibited the calculated spectrum for a = 0.5 MeV.

The calculated energy levels of  $^{84}$ Kr are shown in Fig. 2 and compared with experiments  $^{1,13}$ ). It can be seen that the ordering of the calculated  $0_2^+$ ,  $2_2^+$  and  $4_1^+$  levels in  $^{84}$ Kr agrees with the observed ones. Besides these three levels known experimentally at an excitation energy of  $\sim 2$  MeV, we also predict possible negative parity states of spin 4 and 5. Although the octupole vibrations are not included in the calculation, the energy of the  $3_1^-$ , state is also fairly well reproduced by the theory.

The components of the wave functions of the  $0_1^+$ ,  $0_2^+$ ,  $2_1^+$ ,  $2_2^+$ ,  $2_3^+$ ,  $2_4^+$ ,  $3_1^+$ ,  $4_1^+$ ,  $4_2^+$ ,  $1_1^+$  levels in  $^{84}$ Kr which contributed

more than 4% are listed in Table II. It appears that the ground state has mainly a two-particle configuration, while the remaining states have mixed characteristics.

Experimental information on the multipole mixing ratios  $\delta(\text{E2/Ml})$  are displayed in Table III. We also show the theoretical results, which were obtained by associating with the experimentally observed states  $2^{\pm}(2.759~\text{MeV})$ ,  $3^{\pm}(3.082~\text{MeV})$  and  $1^{\pm}(3.366~\text{MeV})$ , the calculated levels  $2^{+}_{4}(2.79~\text{MeV})$ ,  $3^{+}_{1}(3.40~\text{MeV})$  and  $1^{+}_{1}(3.49~\text{MeV})$ , respectively. By inspecting the experimental and theoretical results one sees that the measured ratios  $\delta(\text{E2/Ml})$  for the cascades  $2^{+}_{2} + 2^{+}_{1} + 0^{+}_{1}$  and  $2^{+}_{3} + 2^{+}_{1} + 0^{+}_{1}$  are reproduced by the calculation. On the contrary, for the remaining four cascades the calculated results for the mixing ratios disagree with the experimental data not only in sign but also in magnitude. This fact may indicate that the measured levels at 2.759 MeV, 3.082 MeV and 3.366 MeV carry negative parity.

In  $^{84}$ Kr nucleus the  $2_1^+$  state is a two-particle cluster of seniority zero coupled to one phonon, while the  $2_2^+$  state is a two-particle cluster of seniority two. The same situation may be found in other vibrational nuclei, as for example in Cd isotopes. This is a consequence of the fact that in these nuclei the lowest single-particle states are of higher spin and, therefore, the pairing energy is large, depressing the multiplets below the broken pairs. Lowest order processes contributing to the  $<\mathbf{I_i} \mid \mid \mathbf{M}(\mathbf{E2}) \mid \mid \mathbf{I_f} >$  and  $<\mathbf{I_i} \mid \mid \mathbf{M}(\mathbf{M1}) \mid \mid \mathbf{I_f} >$  matrix elements are represented, respectively, by diagrams displayed in Fig. 3a and 3b. In the first case, for

each single-particle diagram drawn on the left side correspond three induced collective diagrams drawn on the right-hand side, with all possible time-orderings of the emission or absorption of the virtual phonon. When the angular-momentum algebra is elaborated analytically the mixing ratio can be expressed in the form

$$v = \frac{2}{3} \sqrt{\frac{5}{7}} \frac{(2j+5)(2j-3)}{2j(2j-1)} \frac{\Delta}{\hbar \omega} \frac{Q^{SP}(j)}{g_{R} - g_{j}^{SP}} e_{eff}$$
 (9)

where the symbol j stands for the angular momentum of the dominant single particle-state (j =  $g_{9/2}^{-1}$  for  $^{84}$ Kr and  $^{114}$ Cd),  $^{1}$  is one-particle pairing energy and can be approximated as  $^{14}$ 

$$\Delta \approx \frac{12}{\lambda^{1/2}} \text{ MeV} , \qquad (10)$$

 $\varrho^{\text{SP}}(j)$  and  $g_{\,j}^{\,\text{SP}}$  are, respectively, the single-particle quadrupole moment and the gyromagnetic ratio of the state j, and

$$e_{\text{eff}} = e_{\text{p}}^{\text{eff}} + \frac{5a}{4\sqrt{\pi}} \frac{\hbar \omega}{\Lambda (\hbar \omega - \Lambda)} e_{\text{v}}^{\text{eff}}$$
(11)

is an effective charge.

With the above mentioned parameters we obtain from (9) a value of  $\mathcal{D}=0.56$  while the exact result is  $\mathcal{D}=0.94$ . In a similar calculation performed for the  $^{114}\mathrm{Cd}$  nucleus, with the usual parametrization  $^{2)}$ , expression (9) yields a value  $\mathcal{D}=-0.83$  which should be compared with the exact value  $\mathcal{D}=-1.54$  and the experimental result  $^{15)}$   $\mathcal{D}=-2.2^{+0.7}_{-0.3}$ . Therefore, we can conclude that the higher-order terms, contributing to both the E2 and M1 transition moments and not included in the approximation (9) for

the ratio D, give rise to a change in magnitude but not in sign.

It is worth noting that recently Paar  $^{16}$  has discussed, within the particle-vibration coupling model, the E2/M1 mixing rations in odd-mass spherical and transitional nuclei. He obtained, for example, that for transitions of the type  $\Delta N = 0$  between unique-parity yrast states

$$\mathcal{D}(j+2N+j+2N-1) = \frac{\sqrt{5}}{2j} \left(\frac{2j+4N+2}{2j+4N-2}\right)^{1/2} \frac{Q^{SP}(j)}{g_{j}^{SP}-g_{R}} e_{eff}$$
 (12)

with

$$e_{\text{eff}}^{i} = e_{p}^{\text{eff}} + \frac{5}{\sqrt{\pi}} \frac{a}{\hbar \omega} e_{v}^{\text{eff}}$$
 (13)

Therefore from (9) and (12) we can relate now the ratios of the odd-mass nuclei with those of the neighbouring even-mass nuclei.

#### IV. CONCLUSIONS

We have demonstrated that the property of the  $^{84}$ Kr nucleus arises from neutron hole cluster with the quadrupole vibrational fields. Within this picture the experimentaly energy spectrum and the mixing ratios  $_{6}$ (E2/M1) for the cascades  $_{2}^{+}$   $_{2}^{+}$   $_{1}^{+}$   $_{1}^{+}$  and  $_{3}^{+}$   $_{1}^{+}$   $_{1}^{+}$  are well reproduced.

In addition, a simple rule for the sign and magnitude of the ratio D is given for the vibrational nuclei in which the  $2_1^+$  and  $2_2^+$  states are, respectively, a two-particle

cluster of seniority zero coupled to one phonon and a two--particle cluster of seniority two.

#### ACKNOWLEDGMENTS

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#### FIGURE CAPTIONS

- Fig. 1 Comparison of experimental levels of  $^{83}$ Se (ref. 12),  $^{85}$ Kr (ref. 10),  $^{87}$ Sr (ref. 9),  $^{89}$ Zr (ref. 12) and  $^{91}$ Mo (ref. 11) with the calculated spectra.
- Fig. 2 Experimental $^{1,13}$ ) and calculated level schemes for  $^{84}{\rm Kr}.$
- Fig. 3 Lowest order diagrams for the E2 (3a) and M1 (3b) transitions between the states  $2^+_2$  and  $2^+_1$  in  $^{84}{\rm Kr}$ .

TABLE I - Comparison of experimental and theoretical electric quadrupole and magnetic dipole moments for the ground state ( $I^{\pi} = 9/2^{+}$ ) in N = 49 nuclei.

| <del>,</del>        |                                   |        |  |  |  |
|---------------------|-----------------------------------|--------|--|--|--|
|                     | Experiment                        | Theory |  |  |  |
| 21                  | 85 <sub>Kr</sub> 87 <sub>Sr</sub> |        |  |  |  |
| Q(eb)               | 0.43 a) 0.335 ± 0.020 b)          | 0.37   |  |  |  |
| μ (μ <sub>N</sub> ) | 1.005 a) 1.0924 ± 0.0007 b)       | 1.06   |  |  |  |

a) Ref. 10 , b) Ref. 9.

TABLE II - Wave functions of a few low-lying states in  $^{84}{\rm Kr.}$  Only those amplitudes which are larger than 4% are listed.

| 01   |                                  |                                | 0 2  |               |
|--|----------------------------------|--------------------------------|--|---------------|
| (g <sub>9/2</sub> ) <sup>2</sup>   | 0,00>                            | 0.76                           | (g <sub>9/2</sub> ) <sup>2</sup> 0,00>   | 0,33          |
| $ (p_{1/2})^2$   | 0,00>                            | -0.26                          | (p <sub>1/2</sub> ) <sup>2</sup> 0,00>   | 0.44          |
| (p <sub>3/2</sub> ) <sup>2</sup>   | 0,00>                            | -0.24                          | (p <sub>1/2</sub> ) <sup>2</sup> 0,020>  | 0.23          |
| (f <sub>5/2</sub> ) <sup>2</sup>   | 0,00>                            | -0.25                          | (g <sub>9/2</sub> ) <sup>2</sup> 2,12>   | 0.30          |
| (g <sub>9/2</sub> ) <sup>2</sup>   | 2,12>                            | 0.34                           | (p <sub>1/2</sub> , p <sub>3/2</sub> ) 2,12>   | -0.35         |
| • -  |                                  | -                              | (p <sub>1/2</sub> , p <sub>5/2</sub> ) 2,12>   | -0.36         |
|  |                                  |                                |  |               |
| 21   |                                  |                                | 2+   |               |
| 2 <sup>+</sup> <sub>1</sub>  | 0,12>                            | 0.66                           | 2 <sup>+</sup> <sub>2</sub>  | -0.24         |
|  |                                  |                                | (p <sub>1/2</sub> ) <sup>2</sup> 0,12>   | -0.24<br>0.38 |
| (g <sub>9/2</sub> ) <sup>2</sup>   | 0,12>                            |                                | (p <sub>1/2</sub> ) <sup>2</sup> 0,12>   |               |
| (g <sub>9/2</sub> ) <sup>2</sup><br>  (p <sub>1/2</sub> ) <sup>2</sup>                                       | 0,12><br>0,12>                   | -0.25                          | $ (g_{1/2})^2 $ 0,12><br>$ (g_{9/2})^2 $ 0,22><br>$ (g_{9/2})^2 $ 2,00><br>$ (g_{9/2})^2 $ 2,12> | 0.38          |
| (g <sub>9/2</sub> ) <sup>2</sup><br>  (p <sub>1/2</sub> ) <sup>2</sup><br>  (p <sub>3/2</sub> ) <sup>2</sup> | 0,12><br>0,12><br>2,00><br>2,24> | -0.25<br>-0.21<br>0.37<br>0.22 | $ (p_{1/2})^2 $ 0,12><br>$ (g_{9/2})^2 $ 0,22><br>$ (g_{9/2})^2 $ 2,00>                          | 0.38          |

| 2 4 3  |       |    | 24   |       |
|--|-------|----|--|-------|
| (g <sub>9/2</sub> ) <sup>2</sup> 0,22>               | -0.52 | ÷  | (p <sub>1/2</sub> , f <sub>5/2</sub> ) 2,00> | -0.22 |
| (p <sub>1/2</sub> ) <sup>2</sup> 0,22>               | 0.21  | ÷  | (p <sub>1/2</sub> , p <sub>3/2</sub> ) 2,00> | -0.26 |
| (g <sub>9/2</sub> ) <sup>2</sup> 2,00>               | -0.50 |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,22>       | 0.20  |
| (g <sub>9/2</sub> ) <sup>2</sup> 4,12>               | -0.35 |    | (g <sub>9/2</sub> ) <sup>2</sup> 0,12>       | 0.46  |
|  |       |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,00>       | -0.21 |
|  |       |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,12>       | 0.31  |
|  |       |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,24>       | 0.20  |
|  | . *   |    | (p <sub>1/2</sub> ) <sup>2</sup> 0,12>       | 0.22  |
|  |       |    | <br> (g <sub>9/2</sub> ) <sup>2</sup> 0,22>  | 0.21  |
| - 13<br>- 13 - 14 - 15 - 15 - 15 - 15 - 15 - 15 - 15 |       |    |  |       |
| 41   |       |    | 11   |       |
| $\left  (g_{9/2})^2 \right ^2$ 0,24>                 | 0.43  |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,12>       | 0.78  |
| (g <sub>9/2</sub> ) <sup>2</sup> 2,12>               | 0.47  |    | (g <sub>9/2</sub> ) <sup>2</sup> 2,22>       | -0.22 |
| (g <sub>9/2</sub> ) <sup>2</sup> 4,00>               | 0.57  | ** | \(g <sub>9/2</sub> ) <sup>2</sup> 4,24>      | 0.53  |
| $ (g_{9/2})^2 ^2$ 6,12>                              | 0.22  |    |  | •     |

| 31                                     |       | 4 2                                    |       |
|--|-------|--|-------|
| (g <sub>9/2</sub> ) <sup>2</sup> 0,33> | -0.27 | (g <sub>9/2</sub> ) <sup>2</sup> 0,24> | 0.47  |
| (g <sub>9/2</sub> ) <sup>2</sup> 2,12> | 0.64  | (P <sub>1/2</sub> ) <sup>2</sup> 0,24> | -0.28 |
| (g <sub>9/2</sub> ) <sup>2</sup> 2,22> | 0.40  | (p <sub>3/2</sub> ) <sup>2</sup> 0,24> | -0.21 |
| (g <sub>9/2</sub> ) <sup>2</sup> 2,24> | -0.28 | (g <sub>9/2</sub> ) <sup>2</sup> 4,00> | -0.56 |
| (g <sub>9/2</sub> ) <sup>2</sup> 4,12> | 0.29  | (g <sub>9/2</sub> ) <sup>2</sup> 6,12> | -0.24 |
| (g <sub>9/2</sub> ) <sup>2</sup> 4,22> | 0.22  | (f <sub>5/2</sub> ) <sup>2</sup> 0,24> | -0.21 |
| $ (a, 1)^2   4   24>$                  | 0.20  |  | *     |

TABLE III - Comparison of the experimental and theoretical multipole mixing ratios. The calculated results for the last four cascades were obtained by assuming that the experimentally observed states  $2^{\frac{1}{2}}(2.759 \text{ MeV})$ ,  $3^{\frac{1}{2}}(3.082 \text{ MeV})$  and  $1^{\frac{1}{2}}(3.366 \text{ MeV})$  correspond respectively to the theoretical levels  $2^{\frac{1}{4}}_4(2.79 \text{ MeV})$ ,  $3^{\frac{1}{4}}_1(3.40 \text{ MeV})$  and  $1^{\frac{1}{1}}_1(3.49 \text{ MeV})$ .

| CASCADE                                    |  |                            | Multipole mixing ratio<br>Experimental | &(E2/M1)<br>Theory |
|--|--|----------------------------|--|--------------------|
| 2 <sup>+</sup> (1.898 MeV) →               | 2 <sup>+</sup> (0.882 MeV) +           | 01                         | 0.80 ± 0.03                            | . 0.75             |
| $2^{+}_{3}(2.623 \text{ MeV}) \rightarrow$ | 2 <sup>+</sup> (0.882 MeV) →           | 01                         | -1.05 ± 0.07                           | -0.79              |
| 2 <sup>±</sup> (2.759 MeV) →               | 2 <sup>+</sup> (0.882 MeV) +           | 01                         | -0.07 ± 0.03                           | 0.32               |
| 3 <sup>±</sup> (3.082 MeV) →               | 4 <sup>+</sup> (2.095 MeV) +           | 2 <sup>+</sup> (0.882 MeV) | -0.08 ± 0.01                           | 0.82               |
| 3 <sup>+</sup> (3.082 MeV) →               | $4_2^+(2.348 \text{ MeV}) \rightarrow$ | 2 <sup>+</sup> (0.882 MeV) | -0.07 <sup>±</sup> 0.01                | 0.17               |
| . <del>+</del> (3.366 MeV) →               | 2 <sup>+</sup> (0.882 MeV) +           | 01                         | +0.01 ± 0.01                           | -0.94              |

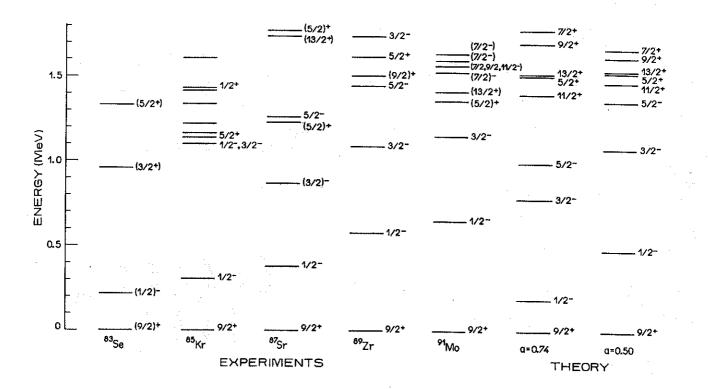


Fig. 1

