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NEAR BARRIER FUSION OF NEUTRON RICH  
PROJECTILES WITH HEAVY TARGET NUCLEI

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# NEAR BARRIER FUSION OF NEUTRON RICH PROJECTILES WITH HEAVY TARGET NUCLEI

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[Invited Talk at the Notre Dame Workshop on Giant Resonances and Related Phenomena, October 21-23, 1991, Notre-Dame, Indiana, USA.]

**Abstract:** The cross-sections for the fusion of  $^{11}\text{Li}$  with  $^{208}\text{Pb}$  and  $^{238}\text{U}$  are calculated at near-barrier energies. The coupling of the entrance channel to the soft giant dipole resonance in  $^{11}\text{Li}$  is taken into account together with the coupling to the break-up channel  $^{9}\text{Li} + 2\text{n}$ . The deformation of  $^{238}\text{U}$  is also considered. The cross-section is found to exhibit important structure around the barrier.

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Supported in part by CNPq.

## Introduction

Recently, the low energy fusion of radioactive beams, such as  $^{11}\text{Li}$ , with heavy target nuclei has been discussed<sup>1-4</sup>). The principal motivation is twofold: i) the enhancement of the fusion cross-section  $\sigma_f$  that arises from the existence of the halo neutrons can be used to further understand these exotic nuclei, ii) the potential production of superheavy cold compound nuclei, with a reasonably measurable cross-sections.

In the calculations made so far, two features of the halo are taken into account: the lowering of the static Coulomb barrier and the coupling of the entrance channel to the low lying soft giant resonance (the pygmy resonance). Both of these effects lead to an enhanced fusion cross-section.

The existence of the pygmy resonance at about 1.2 MeV has recently been firmly established though the study of the double charge exchange reaction  $^{11}\text{B}(\pi^-, \pi^+)^{11}\text{Li}$ <sup>5</sup>). One anticipates, on general ground, that this state has a large width due to the very low binding energy of the dineutron ( $\sim 0.2$  MeV). Thus it is of great importance in any fusion calculation to consider the finite lifetime of the pygmy resonance. This leads to an enhancement of  $\sigma_f$  reduced with respect to that already reported. The purpose of this talk is to consider the above effect by coupling the pygmy resonance to the break-up channel in the calculation of the fusion cross-section.

In what follows are copies of the transparencies that I used in my talk at the Notre Dame Workshop on Giant Resonances and Related Phenomena that was held in Notre Dame, Indiana, October 21-23. My talk is based on several publications by my colleagues in Rio and São Paulo, and I. Ref. 6 above concerns the  $^{11}\text{Li}$  fusion.

November/1991

References

1. A.S. Ilginov, M.V. Mebel and E.A. Cherespanov, Proceedings of the Berkeley Conference on Radioactive Beams (World Scientific) pg. 289.
2. M.S. Hussein, *Phys. Rev. C44* (1991) 446.
3. M.S. Hussein, *Nucl Phys. A531* (1991) 192.
4. N. Takigawa and H. Sagawa, *Phys. Lett. B265* (1991) 23.
5. T. Kobayashi et al. contributions to the Symposium on Structure and Reactions of Unstable Nuclei, June 17-19, 1991, Niigata, Japan, pg. 28.
6. M.S. Hussein, M.P. Pato, L.F. Canto and R. Donangelo, IFUSP/P-942 and submitted for publication.
7. L.F. Canto, R. Donangelo and M.S. Hussein, *Nucl. Phys. A529* (1991) 243.
8. L.F. Canto, R. Donangelo, M.S. Hussein and M.P. Pato, submitted to *Nucl. Phys. A*.

Sub Barrier Fusion Induced by Neutron Rich Nuclei

Canto, Donangelo, Pato, M.S.H.

- Short summary of general features of the structure of neutron-rich nuclei : The pygmy resonance
- Important reactions : break-up
- Coupled channels effects on sub barrier fusion of HI systems
- Effect of pygmy resonance on fusion of exotic (neutron-rich) nuclei with spherical and deformed heavy targets.
- Future directions and general conclusions.

Phys. Rev. C (July)      Phys. Rev. Lett.  
Nuclear Physics (near future)

$^{11}\text{Li}$ : A reasonably well studied system

- Large Coulomb dissociation cross section

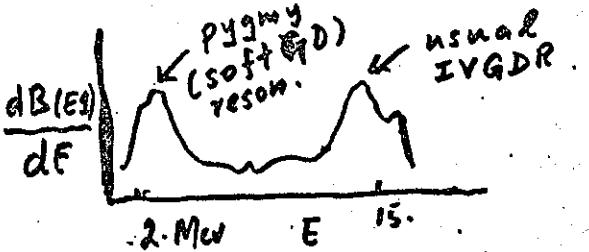
- Evidence for halo neutrons (from break-up study of  $^{11}\text{Li} \rightarrow ^9\text{Li} + 2n$ )



- Very small  $2n$  separation energy (0.2 Mev) and about 2.0 Mev one neutron separation energy

- Spin of  $^{11}\text{Li}$  is  $3/2$  (the ang. mom. of the  $p_{3/2}$  proton in  $^9\text{Li}$ )

- great collectivity at low exc. energy



Within a cluster model ( $^{11}\text{Li} = ^9\text{Li} + 2n$ ) one has

$$\rightarrow \frac{dB(E1)}{dE^*} = \frac{3\hbar^2 e^2}{\pi^2} \frac{Z^2 \Delta N}{AA_c} \sqrt{E} \frac{(E^* - E)^{3/2}}{E^{*4}}$$

sep. energy

exc. neutrons

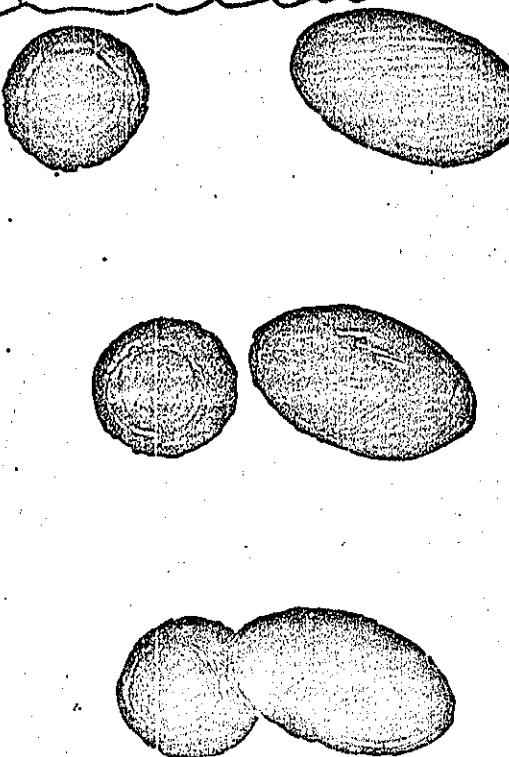
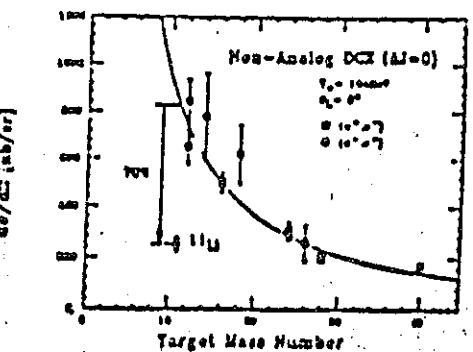
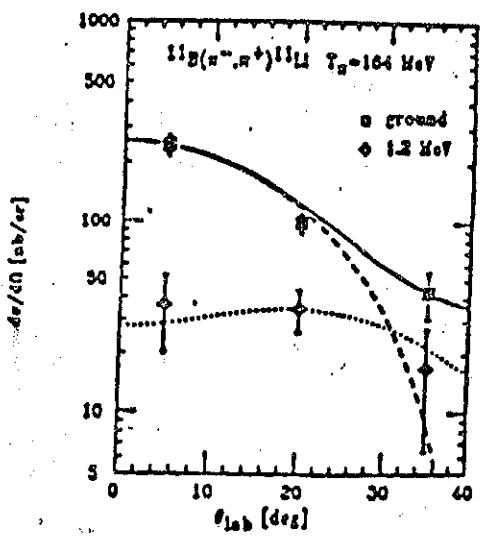
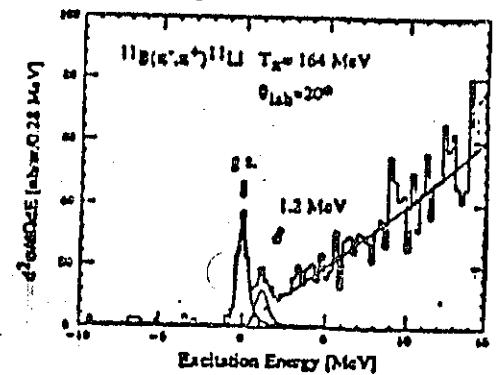
important

$$\rightarrow B(E1) = \frac{3\hbar^2 e^2}{16\pi} \frac{Z^2 \Delta N}{AA_c} \frac{1}{E^4}$$

This coupling ( $\propto B(E1)$ ) goes with with  $B(E1)$  and smaller  $E$

{Smaller, restoring force  
Weaker}

## Fusion Of Neutron-Rich Nuclei



The system feels stronger nuclear attraction

Result: larger fusion probability at low energies (even with spherical targets)

Coupling of entrance channel to low-lying pygmy resonance and to the deformed target (rotor)!

Coupled-Channels Effects on  
Sub Barrier Fusion of HI Systems

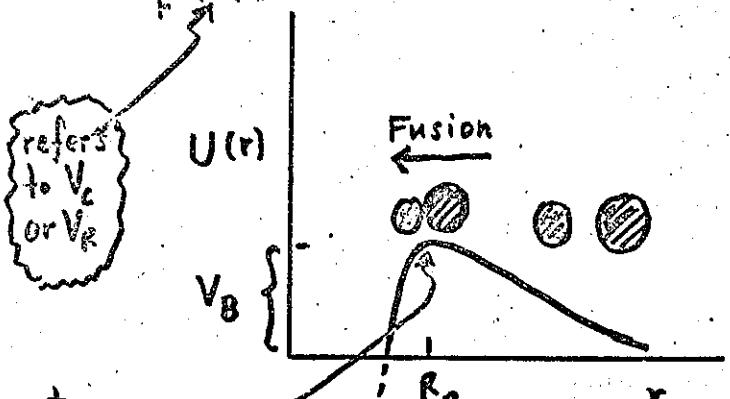
Vibrational coupling :  $V_v$

Rotational coupling :  $V_R$

Purely spherical case ( $V_v = V_R = 0$ )

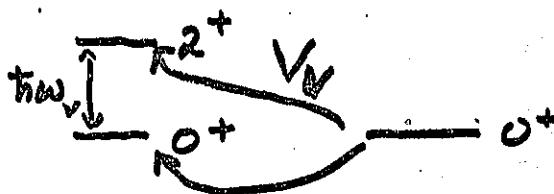
$$\hat{\sigma}_F = \frac{\hbar\omega R_B^2}{2E} \ln \left[ 1 + \exp \left[ \frac{E - V_B}{\hbar\omega/2\pi} \right] \right]$$

$$= \hat{\sigma}_F(\gamma)$$



$\hbar\omega$ :  
Curvature  
of Barrier

VIBRATIONAL CASE



For the fusion cross-section  
in the sudden limit,  $\hbar\omega_v \gg 0$ ,  
one has :

$$\hat{\sigma}_F = \frac{1}{2} \left[ \hat{\sigma}_F(V_v) + \hat{\sigma}_F(-V_v) \right]$$

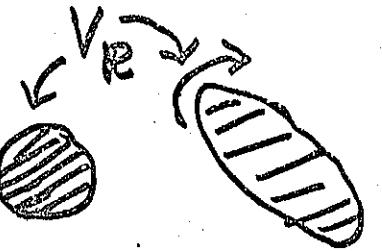
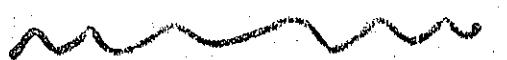
$$\hat{\sigma}_F(V_v) = \frac{\hbar\omega R_B^2}{2E} \ln \left[ 1 + \exp \left[ \frac{E - V_B - V_v}{\hbar\omega/2\pi} \right] \right]$$

At very low energies :

$$\hat{\sigma}_F(V_v) \rightarrow \frac{\hbar\omega R_B^2}{4E} \exp \left[ \frac{2\pi}{\hbar\omega} (E - V_B + V_v) \right]$$

$$\text{Enhancement : } E = \frac{\hat{\sigma}_F}{\hat{\sigma}_F^0} = \frac{1}{2} \exp \left[ \frac{2\pi}{\hbar\omega} V_v \right]$$

Rotational case



take only  $\sigma^+$  and  $\pi^+$  states of the rotor (deformed target)

$$\sigma_F = 0.652 \overset{\circ}{\sigma}_F (0.73 V_R) + 0.348 \overset{\circ}{\sigma}_F (-1.37 V_R)$$

At very low energies,

$$\sigma_F \sim 0.348 \frac{\hbar \omega R^2}{2 E} \exp \left[ \frac{2\pi}{\hbar \omega} (E - V_B + 1.37 V_R) \right]$$

Enhancement

$$E = 0.348 \cdot \exp \left[ \frac{2\pi}{\hbar \omega} (1.37) V_R \right]$$

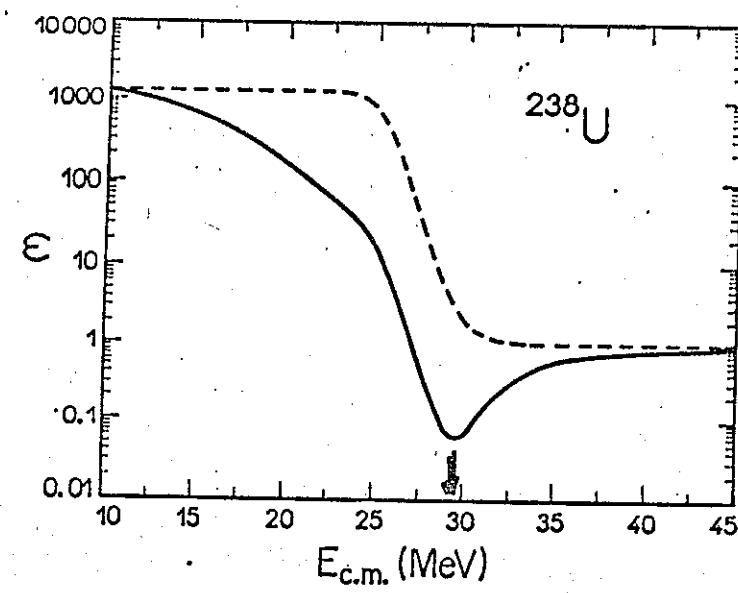
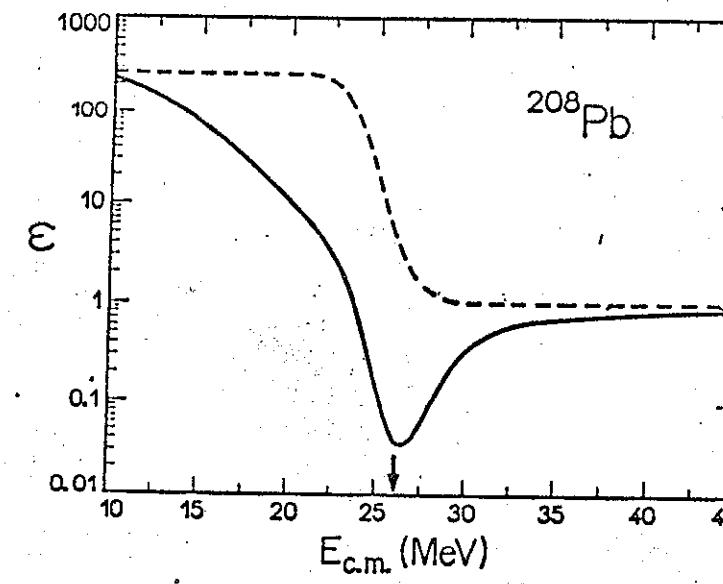
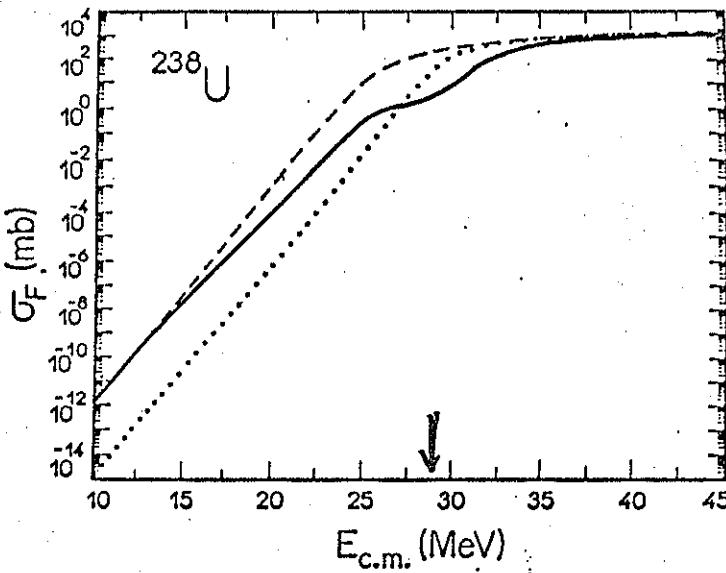
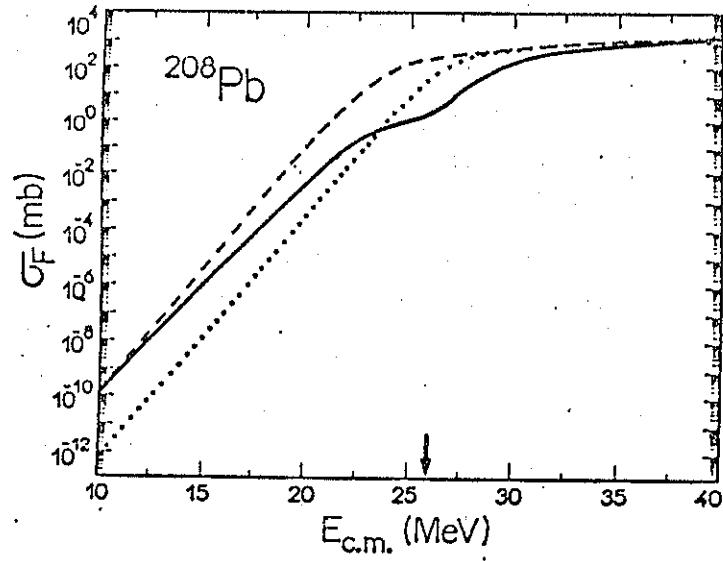
Need more detailed calculation that includes the possibility of the projectile breaking-up. Namely how to couple a resonating state to the entrance channel in a sub-barrier fusion calculation.

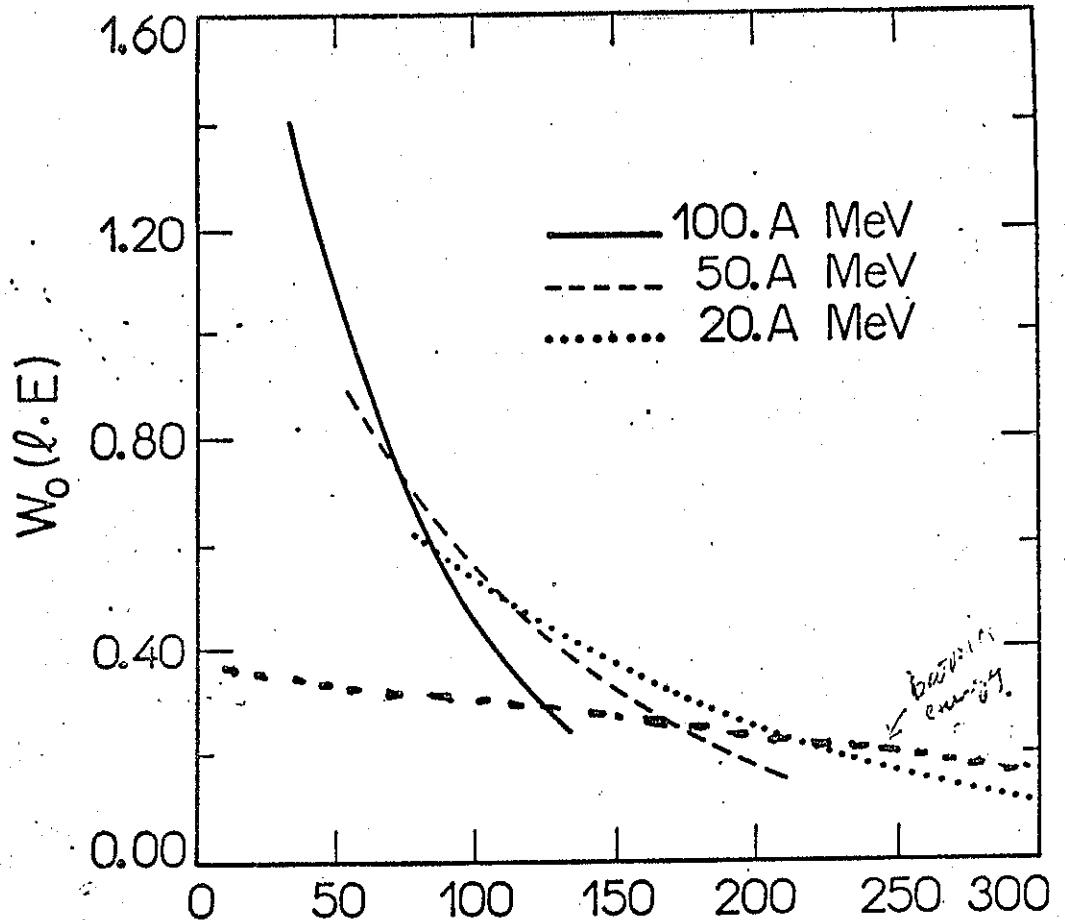
$$\text{Do } \sigma_F = \sum_l P_{\text{b-up}}^{(l)} \sigma_l$$

$$\text{where } P \propto P_{\text{b-up}}^{(l)}$$

width of the pygmy resonance

Use dynamic polarization potential for b-up effects. Results:





Dynamic polarization potential  
in  $^{11}\text{Li} + \text{Pb}$ . FIG. 1 May supply  
 $\Gamma \sim 2 \text{Im } V = 2 \bar{W}_0$  the width  
 $\sim 1.0 \text{ Mev.}$  of the pygmy  
resonance